

CÁLCULO DE LÍMITES.

Ejercicio 5:

a) $\lim_{x \rightarrow 0} (x^3 - x^2 + 1) =$

c) $\lim_{x \rightarrow 2} 4 =$

e) $\lim_{x \rightarrow 0} \left(4 + \frac{1}{x^2} \right) =$

g) $\lim_{x \rightarrow 0} \left(x - 4 - \frac{1}{x^2} \right) =$

i) $\lim_{x \rightarrow 0} \left(\frac{2}{x^4} + \frac{1}{x^2} \right) =$

k) $\lim_{x \rightarrow 0} \left(2 + \frac{1}{x^2} \right) =$

m) $\lim_{x \rightarrow 2} [x^2 \cdot (x + 3)] =$

ñ) $\lim_{x \rightarrow 2^+} \left[3x \cdot \frac{1}{x-2} \right] =$

p) $\lim_{x \rightarrow 2} [(x^2 - 4) \cdot (x + 2)] =$

r) $\lim_{x \rightarrow 2} \left[(x^2 - 4) \cdot \frac{1}{x-2} \right] =$

t) $\lim_{x \rightarrow 0^+} \left[\frac{1}{x^2} \cdot x \right] =$

v) $\lim_{x \rightarrow 0^-} \left[\frac{-3}{x} \cdot (3x + 5) \right] =$

x) $\lim_{x \rightarrow 3^-} \left[\frac{1}{x-3} \cdot \frac{-2}{x-3} \right] =$

z) $\lim_{x \rightarrow 0^-} \left[\frac{1}{x^2} \cdot (x^2 - 1) \right] =$

bb) $\lim_{x \rightarrow 5} \frac{x^2 + 5}{x - 3} =$

b) $\lim_{x \rightarrow 3} (x^2 + 1) =$

d) $\lim_{x \rightarrow 1} (x - 3) =$

f) $\lim_{x \rightarrow 0} \left(3x + 2 + \frac{1}{x^4} \right) =$

h) $\lim_{x \rightarrow 0} \left(3x + 2 - \frac{5}{x^4} \right) =$

j) $\lim_{x \rightarrow 0^+} \left(\frac{1}{x} - \frac{2x+1}{x} \right) =$

l) $\lim_{x \rightarrow 0^+} \left(\frac{1}{x^5} - \frac{1}{x^4} \right) =$

n) $\lim_{x \rightarrow 2} [(x - 2) \cdot 6x] =$

o) $\lim_{x \rightarrow 2^+} \left[(x - 4) \cdot \frac{1}{x-2} \right] =$

q) $\lim_{x \rightarrow 2} [(x^2 - 4) \cdot (x - 2)] =$

s) $\lim_{x \rightarrow 0} \left[\frac{1}{x^2} \cdot 3x^2 \right] =$

u) $\lim_{x \rightarrow 2^-} \left[(x^2 - 5) \cdot \frac{1}{x-2} \right] =$

w) $\lim_{x \rightarrow 2^+} \left[\frac{2}{x^2 - 4} \cdot \frac{1}{x-2} \right] =$

y) $\lim_{x \rightarrow 0^+} \left[\frac{1}{x} \cdot (x^2 + x) \right] =$

aa) $\lim_{x \rightarrow 5} \frac{x^3 + 1}{x} =$

cc) $\lim_{x \rightarrow 3} \frac{x^2 - 9}{x + 3} =$

Ejercicio 6:

a) $\lim_{x \rightarrow 1} \frac{2x - 3}{(x + 1)^2} =$

b) $\lim_{x \rightarrow 3} \frac{2x - 6}{(x + 1)^2} =$

c) $\lim_{x \rightarrow 2^+} \left[\frac{1}{x-2} : (x+2) \right] =$

d) $\lim_{x \rightarrow 3^+} \left[\frac{1}{x-3} : (x-5) \right] =$

$$e) \lim_{x \rightarrow +\infty} \frac{x^2 + 5}{-3} =$$

$$f) \lim_{x \rightarrow 0^+} \frac{1}{x^3} =$$

$$g) \lim_{x \rightarrow 1} \frac{3}{(x-1)^2} =$$

$$h) \lim_{x \rightarrow 2} \frac{x^2 - x - 2}{x^3 - 2x^2} =$$

$$i) \lim_{x \rightarrow 1^-} \frac{x^3 + 2x^2 - x - 2}{x^3 - x^2 - x + 1} =$$

$$j) \lim_{x \rightarrow 1} \frac{x^2 + x - 2}{x^2 - 2x + 1} =$$

$$k) \lim_{x \rightarrow 1} \frac{x^3 - 1}{(x-1)^2} =$$

$$l) \lim_{x \rightarrow 2} \frac{x^2 - 4x + 4}{x^2 - 4} =$$

$$m) \lim_{x \rightarrow 2} \frac{x^2 - x - 2}{x^2 - 4} =$$

$$n) \lim_{x \rightarrow 2^+} \left[\frac{1}{x-2} : (x^2 - 4) \right] =$$

$$\tilde{n}) \lim_{x \rightarrow 0} \left[\frac{1}{x} : x \right] =$$

$$p) \lim_{x \rightarrow 2^+} \left[(x-2) : \frac{1}{x-2} \right] =$$

$$r) \lim_{x \rightarrow +\infty} (x^2 - x) =$$

$$t) \lim_{x \rightarrow \infty} \frac{3x^3 + 2x^2 - 7}{4x^2 - 5x + 6} =$$

$$v) \lim_{x \rightarrow \infty} \frac{3x^3 - 1}{4x^4 + 5x^2} =$$

$$x) \lim_{x \rightarrow \infty} \frac{4x^2 + 2x + 3}{1 - x^3} =$$

$$z) \lim_{x \rightarrow \infty} \frac{2x + 1}{x^2 - 3x} =$$

$$bb) \lim_{x \rightarrow \infty} \frac{1 + x^5}{x^3} =$$

$$dd) \lim_{x \rightarrow 0} \left(\frac{1}{x} - \frac{1}{x + 3x^2} \right) =$$

$$o) \lim_{x \rightarrow 2^+} \left[(x+2) : \frac{1}{x-2} \right] =$$

$$q) \lim_{x \rightarrow +\infty} \frac{-2}{x^2 - 2x + 1} =$$

$$s) \lim_{x \rightarrow +\infty} (x^2 + x^3) =$$

$$u) \lim_{x \rightarrow \infty} \frac{5x^2 - 1}{3x^2 + 2x + 3} =$$

$$w) \lim_{x \rightarrow \infty} \frac{x^6 + 2x^7}{3x^6 + 2} =$$

$$y) \lim_{x \rightarrow \infty} \frac{4x^3 + 2x - 5}{2x^2 + 5x - x^3} =$$

$$aa) \lim_{x \rightarrow \infty} \frac{x^2 - 4x}{2 - 3x^2} =$$

$$cc) \lim_{x \rightarrow \infty} \frac{4 - x}{x^2 - 1} =$$

$$ee) \lim_{x \rightarrow 0} \left(\frac{x+1}{x^2} - \frac{1}{x^2-x} \right) =$$

$$ff) \lim_{x \rightarrow 1} \frac{\sqrt{x+3} - 2}{x-1} =$$

$$gg) \lim_{x \rightarrow 2} \frac{x-2}{\sqrt{x+2} - 2} =$$

$$hh) \lim_{x \rightarrow 0} \frac{-x}{\sqrt{x+9} - 3} =$$

$$ii) \lim_{x \rightarrow \infty} \sqrt{x^4 + 2x + 7} =$$

Ejercicio 7:

$$a) \lim_{x \rightarrow \infty} \sqrt[3]{-x^5 + 4x + 2} =$$

$$b) \lim_{x \rightarrow +\infty} \sqrt{6x + 2} =$$

$$c) \lim_{x \rightarrow \infty} \frac{\sqrt{x^2 + 2x}}{\sqrt{3x^2 + 2}} =$$

$$d) \lim_{x \rightarrow +\infty} \frac{\sqrt{x^3 + 3x}}{\sqrt{x^2 + 10}} =$$

$$e) \lim_{x \rightarrow \infty} \frac{\sqrt[3]{8x^6 + 9x^5 + 4}}{\sqrt{4x^4 + 10x - 2}} =$$

$$f) \lim_{x \rightarrow \infty} \frac{\sqrt{8x^2 + 2x + 3}}{\sqrt[3]{8x^3 - 5x^2 + 3}} =$$

$$g) \lim_{x \rightarrow \infty} \frac{\sqrt[3]{-3x^3 + 2x - 5}}{\sqrt[3]{2x^2 + 3}} =$$

$$h) \lim_{x \rightarrow \infty} \frac{x-2}{\sqrt[4]{16x^4 + 8}} =$$

$$i) \lim_{x \rightarrow +\infty} (\sqrt{x^4 + 2} + \sqrt{x^3 + 3}) =$$

$$j) \lim_{x \rightarrow +\infty} (\sqrt{x^4 + 2} - \sqrt{x^3 + 3}) =$$

$$k) \lim_{x \rightarrow +\infty} (\sqrt[3]{x^2 + 5} - \sqrt{x^3 + 2}) =$$

$$l) \lim_{x \rightarrow \infty} (\sqrt{4x^2 + 2x} - \sqrt{9x^2 - 3x}) =$$

$$m) \lim_{x \rightarrow \infty} (\sqrt{x^4 - 10x} - \sqrt{x^4 - 5x^2 + 7}) =$$

$$n) \lim_{x \rightarrow +\infty} \frac{1}{\sqrt{x+2} - \sqrt{x-5}} =$$

$$\text{ñ) } \lim_{x \rightarrow +\infty} \left[\frac{2x^2 - 5x + 7}{x + 3} - 2x \right] =$$

$$\text{p) } \lim_{x \rightarrow 1} (3x - 2)^{\frac{x-1}{3x-7}} =$$

$$\text{r) } \lim_{x \rightarrow -3^+} (3x + 9)^{\frac{-3x-1}{3x-7}} =$$

$$\text{t) } \lim_{x \rightarrow 5} (3x - 15)^{x-5} =$$

$$\text{v) } \lim_{x \rightarrow 1} (3x - 2)^{\frac{3x+1}{4}} =$$

$$\text{x) } \lim_{x \rightarrow 0} \left(\frac{7x + 5}{2x + 5} \right)^{\frac{1}{2x}} =$$

$$\text{z) } \lim_{x \rightarrow +\infty} \left(\frac{x^2 + 2}{x + 2} \right)^{\frac{-2x}{x-1}} =$$

$$\text{o) } \lim_{x \rightarrow 5} (3x + 2)^{\frac{3x+1}{3x-7}} =$$

$$\text{q) } \lim_{x \rightarrow 0} \left(\frac{7x + 10}{2x + 5} \right)^{\frac{1}{2x}} =$$

$$\text{s) } \lim_{x \rightarrow +\infty} \left(\frac{x^2 + 1}{2x - 2} \right)^{\frac{-1}{x}} =$$

$$\text{u) } \lim_{x \rightarrow 5^+} (3x - 15)^{\frac{1}{x-5}} =$$

$$\text{w) } \lim_{x \rightarrow 1} (3x - 2)^{\frac{x-1}{4}} =$$

$$\text{y) } \lim_{x \rightarrow +\infty} \left(\frac{x^2 + 2}{x + 2} \right)^{\frac{2x}{x-1}} =$$

Ejercicio 8:

$$\text{a) } \lim_{x \rightarrow +\infty} \left(\frac{x^2 + 1}{2x - 2} \right)^x =$$

$$\text{b) } \lim_{x \rightarrow +\infty} \left(\frac{x^2 + 1}{2x - 2} \right)^{-x} =$$

$$\text{c) } \lim_{x \rightarrow 3} f(x) \text{ siendo } f(x) = \begin{cases} \frac{x+3}{x+2} & \text{si } x \geq 1 \\ \frac{2x-1}{x+2} & \text{si } x < 1 \end{cases}$$

$$\text{d) } \lim_{x \rightarrow -1} f(x)$$

$$\text{e) } \lim_{x \rightarrow 1} f(x)$$

$$\text{f) } \lim_{x \rightarrow 0} f(x)$$

$$\text{g) } \lim_{x \rightarrow -1} g(x) \text{ siendo } g(x) = \begin{cases} \frac{1}{x} & \text{si } x > 0 \\ 2x - 3 & \text{si } x \leq 0 \end{cases}$$

$$\text{h) } \lim_{x \rightarrow 0} g(x)$$

$$\text{i) } \lim_{x \rightarrow 1} g(x)$$

$$\text{j) } \lim_{x \rightarrow \infty} g(x)$$

$$\text{k) } \lim_{x \rightarrow 1} h(x) \text{ siendo } h(x) = \begin{cases} \frac{x-1}{x^2-1} & \text{si } x \neq 1 \\ 3 & \text{si } x = 1 \end{cases}$$